

Estimates of performance model factors for passive microseismic SADAR phased arrays at the Newell County Facility

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Summary

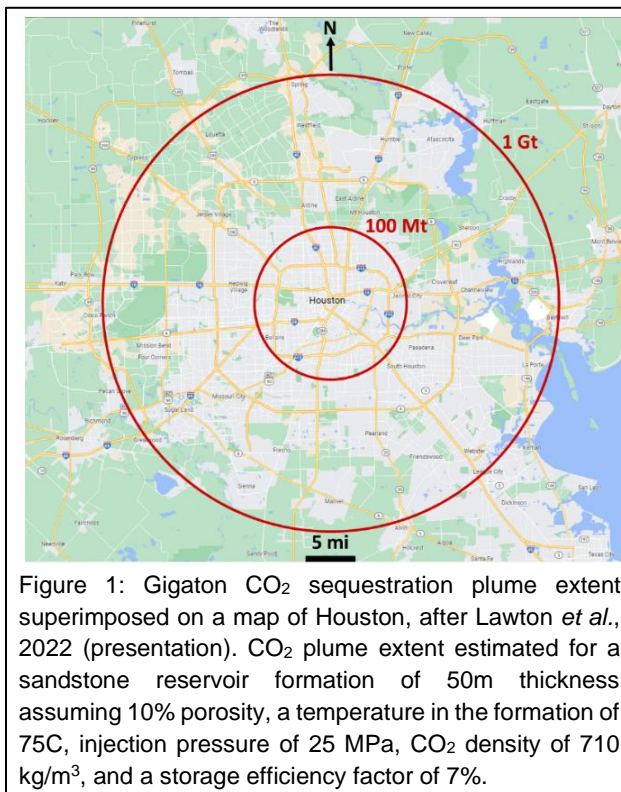
Considering the geographic extent for the large CO₂ geologic sequestration projects required to meet emissions goals, the likewise-required measurement, monitoring, and verification (MMV) technology operations will need to be scalable and cost effective over a duration that extends beyond closure of the reservoir. Networks of passive compact volumetric phased arrays (SADAR arrays) for microseismic monitoring MMV offer superior data acquisition capabilities using a reduced footprint compared to surface deployed arrays, and phased array signal processing methods produce superior results for detecting and locating microseismic events. A sparse network of four SADAR arrays was installed at the Containment and Monitoring Institute developed and operated Newell County Facility in fall of 2021. After summarizing the development of arrays in global and exploration geophysics, we discuss the array design considerations for being able to fully use phased arrays. A mathematical basis for understanding and evaluating SADAR system performance based on the sonar equation is developed. We present observations of noise levels in the frequency domain, and those observations allow several of the factors in the performance model to be estimated, focusing on the measured noise level and the noise suppression useful in determining the array gain. A selection of high-quality events drawn from the SADAR bulletin is used to construct a plot of the measured received-signal-power versus event source-to-receiver range as a function of estimated event magnitude (*i.e.*, source level) in comparison to the measured noise levels also plotted on the graph, showing the basic single channel level and the noise level after coherent processing. From these performance estimates and the results from the bulletin, it is possible to estimate the completeness magnitude of the bulletin at $M_w = -2.5$.

Introduction

Multiple reports have documented the need for capture and storage of CO₂ amounts on the order of tens of gigatons per annum to meet the requirements for worldwide net-emission reductions (IEA, 2020). The International Energy Agency states that CCS needs to reach 5.5. GT of CO₂ capture and stored per year worldwide to meet the net-zero emission by the 2050 target (IEA, 2020, 2021). In light of these goals, geologic carbon storage (GCS) is becoming a required technology for the permanent reduction of carbon dioxide emissions (IPCC, 2021; English and English, 2022). The Global CCS Institute reports for 2021 and 2022 provide summaries and

projections of an increasing number of GCS projects opening in the near future; projects in early development number in the 10s.

Economical and effective measurement, monitoring, and verification (MMV) technologies help manage the risks associated with underground carbon sequestration, ensure ongoing operations, and verify reservoir integrity beyond the reservoir closure. Lawton *et al.*, (2022) recognize that any CCS reservoir containing volumes upwards of 100 Mt will require substantial MMV efforts much in excess of current pilot studies (Figure 1). Furthermore, injecting CO₂ is more complicated than just reversing hydrocarbon production. The CO₂ plume may evolve in ways that models do not predict (Ringrose *et al.*, 2022; Rassenfoss, 2023), and real-time and persistent monitoring is required for detecting transient changes and providing timely information to field operators.



Active and passive seismic methods continue to be tested as fundamental technologies for remote sensing and monitoring of carbon sequestration reservoirs. The economic and logistical realities of required on-going reservoir monitoring warrant permanently installed robust systems with the minimum number of channels, reduced infrastructure requirements, and minimal surface expression (e.g., Eaton, 2018). Such systems are required to be cost effective, reliable, and maintainable for lifetimes extending well past closure of injection. Extensive networks of surface-emplaced seismic geophones are the most common active and passive monitoring deployments for detecting changes in reservoirs associated with engineering activities. Dense deployments of geophones have been reported as the most effective configuration for 4-D monitoring using active surveys or used to monitor hydrofracking operations. However, these survey deployments are usually temporary. Only passive seismic monitoring provides a

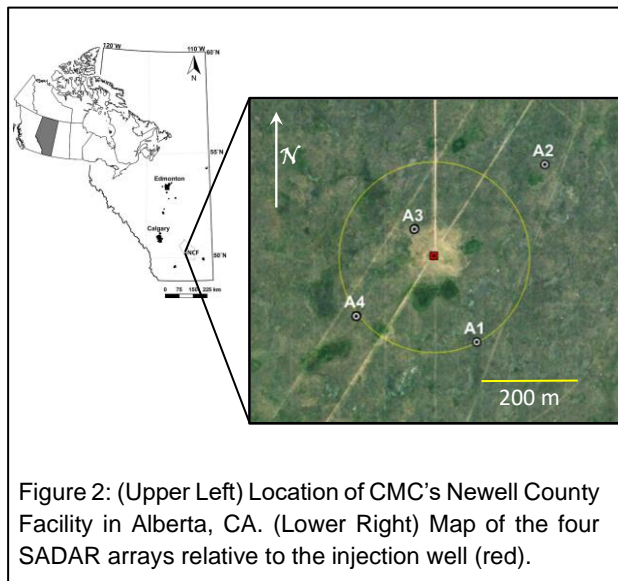
continuous and persistent capability for the sensing and characterization of microearthquakes associated with CO₂ injection, operations, or reservoir failure.

A common approach for detection and location of microseismic events is to use a large network of surface sensors covering the reservoir geographic extent. Noise levels are a primary obstacle and overcoming noise levels using surface arrays demands dense sensor deployments and large channel counts in order to produce a bulletin with magnitudes of completeness below Mw 0 and acceptable horizontal and depth location uncertainties. The daily industrial operations at CCS fields will result in a variety of seismic energy sources distributed in location that create a variety of non-stationary noise signals that tend to be coherent; these coherent noise signals clutter the acquired time series. Surface sensor networks mitigate this noise with sheer numbers, fielding

large and dense networks that allow constructing FK and other spatial filters aimed at specific noise sources. However, for reservoirs at a gigaton scale as shown in Figure 1, the spatial footprint for the required surface sensor network and the number of channels would be incredible for reliably detecting and locating even relatively large Mw 0 events.

The standard alternative to large surface deployments involves vertical line arrays in boreholes close to the injection well and away from surface noise, allowing the detection of more events at lower magnitudes. Using borehole arrays for detection and location of events to a low magnitude of completeness will require instrumenting many boreholes engineered throughout the monitored volume to reservoir depths of ~2 km. The borehole network will also need to monitor the geologic volume above the active reservoir and discriminate between surface activities and real seismic events, requiring additional sensors deployed towards the surface. Reducing noise via deep borehole emplacements will then come at increased cost and complexity compared to surface networks. Nevertheless, for reservoirs at a gigatonne scale as shown in Figure 1, providing the spatial density required for adequate monitoring of the whole reservoir using deep borehole arrays, as well as sustaining the network over the operational life of the field and beyond, will be complicated and expensive.

Networks of SADAR compact volumetric phased arrays are becoming a proven and economical passive monitoring solution offering technical and economic advantages over surface deployments and deep borehole arrays (Zhang *et al.*, 2023; Zhang *et al.*, 2022; Nyffenegger *et al.*, 2022). Quantum Technology Sciences (Quantum) has installed four SADAR arrays configured as a sparse network at Carbon Management Canada's (CMC) Newell County Facility (NCF) in Southern Alberta, demonstrating an effective monitoring capability (Figure 2). Quantum's SADAR® system uses a scalable and configurable network of passive SADAR arrays permanently deployed in the shallow subsurface for automatically detecting and locating microseismic events at depth. SADAR arrays can be tuned to meet the design frequencies and wavelengths specific to the site, optimize the signal-to-noise ratio (SNR) of the received signal,



determine an unambiguous angle-of-arrival, and determine the phase velocity of the arriving signal. In comparison with surface dense or patch seismic deployments, SADAR arrays offer a reduced surface footprint and enhanced signal detection and characterization capabilities. In comparison with borehole arrays, permanent SADAR arrays have a reduced cost for emplacement and more easily accessible and serviced components while still avoiding the majority of the surface noise within the band of interest, and the phased array processing provides superior data quality and physical characteristics of the signal. In terms of the overall network, the SADAR system architecture is designed for permanent and persistent real-time data acquisition and

processing for microseismic monitoring applications, and the SADAR network architecture has the ability to grow incrementally as the state and understanding of the CO₂ plume changes or as the progression of microseismic events dictates so that the monitoring zone remains within the network.

The bulk of this work contains information about the fielded SADAR arrays and a discussion on phased array design, observations of the SNR and location of events, followed by mathematical analysis of the physical and processing system factors affecting performance, and observations of signals and noise for some of the seismic instrumentation at the NCF. An assessment of the noise observations and how the measured noise levels fit into the performance framework follows, as well as an assessment of the noise suppression of the arrays and the performance of received signal versus range for the network of arrays.

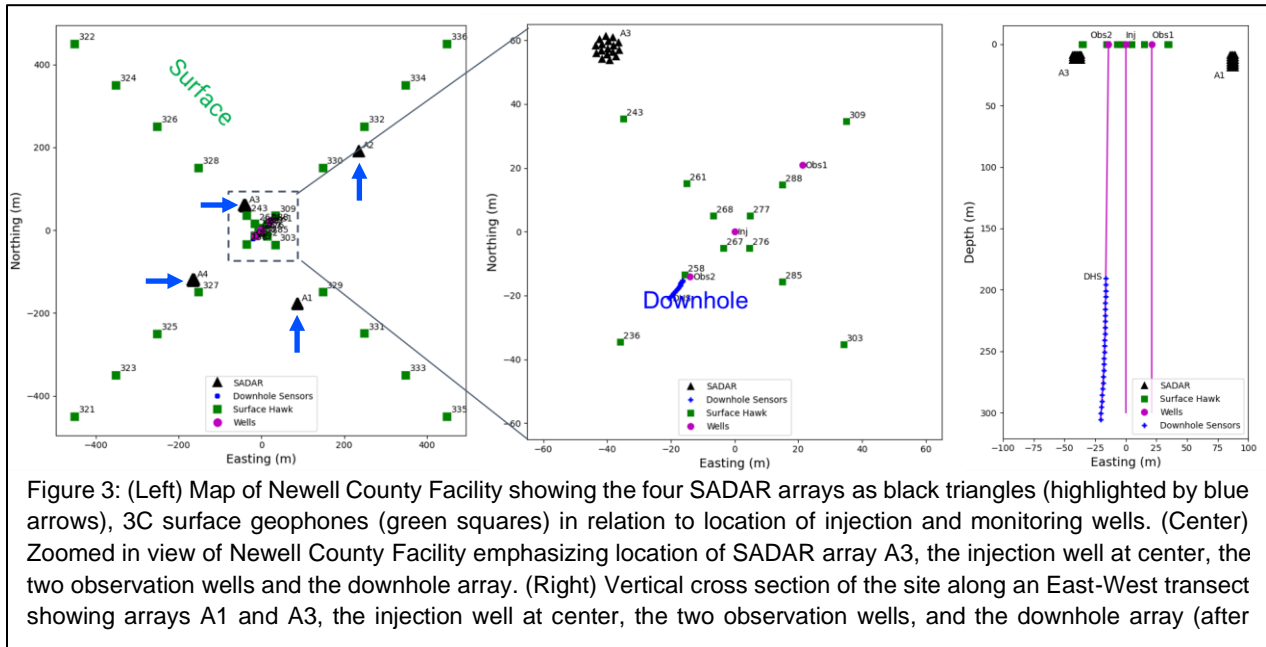
Field Setting

The Containment and Monitoring Institute, a division of Carbon Management Canada (CMC) Research Institutes, in collaboration with the University of Calgary, developed and operates the 200-hectare NCF (Figure 2) located in Southern Alberta, Canada (Lawton *et al.*, 2019). The NCF is currently simulating an unplanned CO₂ leakage from a deeper/larger scale CO₂ storage project via injection of ~10-30 tonnes/year of CO₂ into the Basal Belly River Sandstone (BBRS) reservoir at ~300m depth (Macquet *et al.*, 2022). The BBRS is a well-studied seven-meter thick shoreface horizon composed of sorted quartz grains with ~11% average porosity and with maximum permeability of ~0.8 mD (Dongas and Lawton, 2015; Osadetz *et al.*, 2015; Vocke *et al.*, 2016; Muravieva *et al.*, 2017; Jafari Raad *et al.*, 2021). The Upper Cretaceous Foremost Formation caprock that forms the reservoir seal is a 152 m thick clayey sandstone with interbedded coal layers. The upper ~30 meters above the bedrock is composed of unsorted glacial tills and soils.

The objective for the NCF is the development and improvement of CO₂ measurement, monitoring, and verification (MMV) technologies for minimizing risks associated with geologic CO₂ storage (*e.g.*, containment failure). Simultaneous monitoring at the NCF using multiple networks and sensor types provides a unique opportunity to compare the detection and location performance for a variety of sensor modalities, arrangements, and processing approaches to prioritize those that offer cost-effective and robust verification of CO₂ containment (Lawton *et al.*, 2019; Macquet *et al.*, 2022). For microseismic monitoring specifically, the site features a string of 24 3C geophones within one monitoring well (Figure 3), 7 broadband seismometers emplaced 1m deep, and 28 3C geophones emplaced 1m deep in an “X” configuration centered on the injection well (Figure 3) (Savard *et al.*, 2020).

In November of 2021, Quantum, in cooperation with Newell County Facility management, installed a sparse network of four permanent SADAR compact volumetric phased arrays, shown in Figure 2 and Figure 3, designed specifically for passively monitoring microseismic activity associated with the CO₂ injection activities. Detections on four arrays is the minimum number enabling overdetermined event location procedures that yields both the location and the uncertainties in origin time, horizontal location, and depth. Array A3 is the closest to the injection well at 70m to the north-west, arrays A1 and A4 are located 200m south-west and south-east respectively from the injection well, and array A2 is the furthest at 300m to the north-east from the injection well, all with topmost depths at ~9m and vertical extent contained within the Pleistocene-Holocene sediments and glacial till layer. All elements in all arrays are filled by Geospace GS-ONE 10 Hz

vertical-only geophones, and all are acquired as separate channels at a 2000 samples per second rate.



These four arrays test three different SADAR array designs based on uniform cylindrical array (UCA) geometries with diameters ranging from 4m to 7.5m (Figures 4 and 5). Array design (1) the “Standard” UCA configured as an octagon with a central axis and six uniformly vertically spaced levels, and used in deployed arrays A1 and A2 (located in Figures 2 and 3). Array design (2), shown in Figure 5, is the “Wide Aperture” layout configured to have a larger radius as nested UCAs with the outermost arranged as a decagon and the inner as a hexagon with three uniformly spaced levels, designed with improved aperture for waves with a more vertical incidence balanced with the need for a broad bandwidth response and to separate clutter arriving with a more horizontal incidence, and used in array A3. Array A4, also shown in Figure 5, uses the design (3) “Hybrid” approach combining features of the “Standard” array and the “Wide Aperture” design, with the outer UCA having three levels, and the inner hexagon UCA having six. In addition, at the A2 array, the Quantum installation included a surface tripartite array of Geospace GCL 3C packages using GS-SMG 10 Hz sensors, combined with a single small aperture array at one of the vertexes of the tripartite array all acquiring at 2000 samples per second, to be used as a receiver group mainly for noise comparison purposes (Figure 4). The GCL cluster design intentionally used spacings where low frequency noise should be correlated as a test of noise independence.

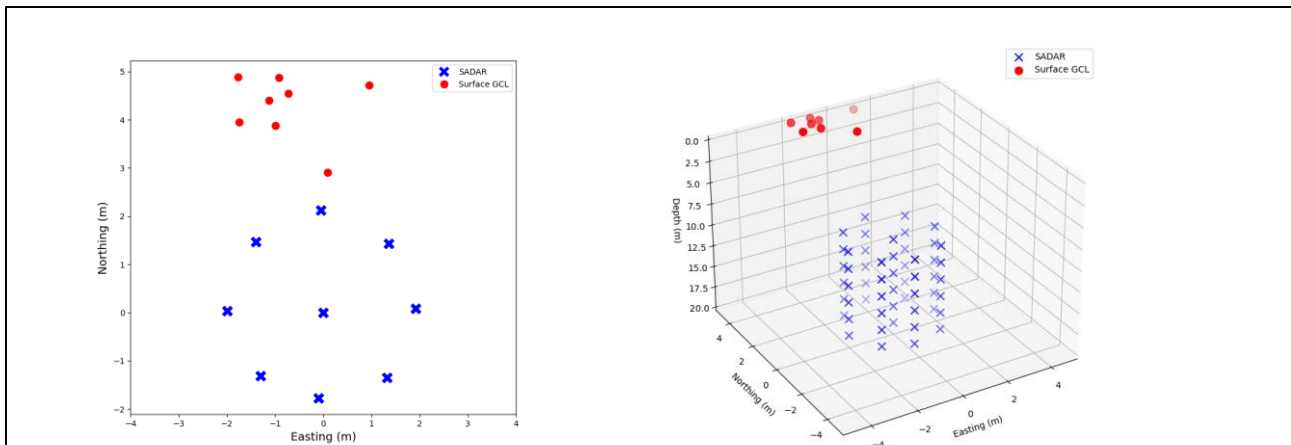


Figure 4: Array design (1) – “Standard” shown at left in map view and right in a three-dimensional view, designed as a uniform cylindrical array with a vertical central axis of configured as an octagon with six levels with uniform spacing of 2m between levels. Design (1) is used for arrays A1 and A2. All array elements are Geospace GS-ONE 10 Hz vertical phones. An additional surface cluster of Geospace GCL units with 10 Hz GS-SMG phones was emplaced above A2 for noise comparisons.

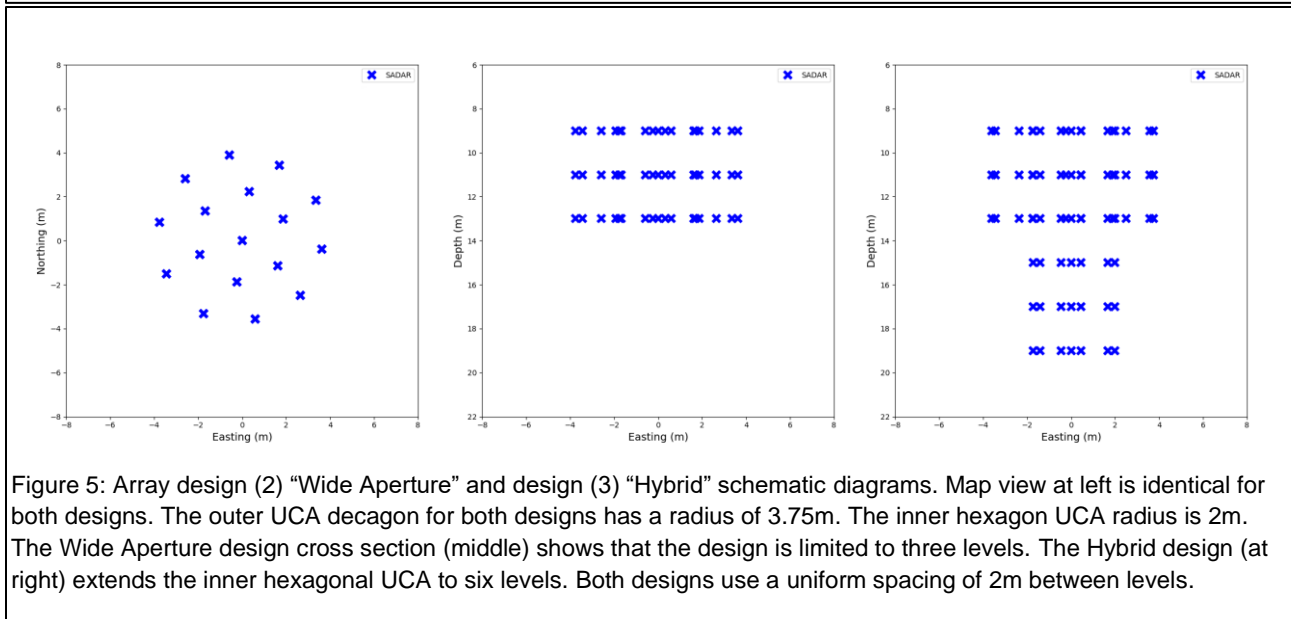


Figure 5: Array design (2) “Wide Aperture” and design (3) “Hybrid” schematic diagrams. Map view at left is identical for both designs. The outer UCA decagon for both designs has a radius of 3.75m. The inner hexagon UCA radius is 2m. The Wide Aperture design cross section (middle) shows that the design is limited to three levels. The Hybrid design (at right) extends the inner hexagonal UCA to six levels. Both designs use a uniform spacing of 2m between levels.

Background

The general technique of arranging Individual sensors into geometric groupings, *i.e.* arrays, has been used in signal acquisition and measurement since around the time of World War-One and is now ubiquitous in virtually every sensing domain that takes advantage of modern digital signal processing. Within this work we use the term *phased array* in the traditional sense described in Van Trees (2002), Frank and Richards (2008), and Ziomek (1995) such that the overall phased array system of sensors and acquisition components enables signal processing methods that take

advantage of the spatial coherence of the signal of interest. The term *coherent processing* here is synonymous with *phased array processing* and reserved exclusively to mean spatially-coherent processing such as beamforming, where signals acquired with a phased array of point sensors are cooperatively manipulated based on the coherence of signals propagating across the array to derive multiple simultaneous directional “beams” specified by the beam main response axis (MRA) pointing outward from a defined reference point. The term *point sensor* is defined such that the dimensions of the sensor are much smaller than the wavelength of the maximum seismic frequency of interest *i.e.* as a sensor that measures the applicable field at a single point rather than as a distributed sensor that integrates signal measurements over a finite aperture. Array elements are the locations of the point sensors, and may be occupied by single sensors, or multiple vector sensors as is the case with triaxial geophone packages.

The signal processing methods for exploiting phased arrays are well-developed across multiple disciplines such as radar (*e.g.*, Skolnik, 2001; Van Trees, 2002), sonar (*e.g.*, Ainslie, 2010; Abraham, 2019), and acoustics (*e.g.*, Mueller, 2002; Michel, 2006;), and for seismology, array processing has a rich history. Both Husebye and Ruud (1989) and Douglas (2013) trace the history of passive seismic phased arrays applied to global nuclear monitoring to the late 1950’s, at about the same time that the US government began project VELA-UNIFORM. Global seismology phased array processing methods and results are now explained in textbooks (*e.g.*, Aki and Richards, 1980; Lay and Wallace, 1995; Ammon *et al.*, 2021), topical monographs and operator manuals (*e.g.*, Havskov and Alguacil, 2006; Havskov and Ottenmoller, 2010; Douglas, 2013; Schweitzer *et al.*, 2012), and subject review papers (*e.g.*, Husebye and Ruud, 1989; Rost and Thomas, 2002).

Global seismic monitoring focuses on detection and characterization of impulsive transient (IT) signals originating with earthquakes and underground nuclear explosions, *i.e.* short duration, broadband signals. Passive undersea monitoring extends the set of signals of interest to include narrow-band signals of prolonged duration commonly called continuous waveforms (CWs) and frequency modulated waveforms (FMs) generated by watercraft. Engine driven and electromechanical equipment commonly used in construction, industrial activities, and everyday society generate similar vibrational signals and it is no surprise that seismic sensing systems also acquire these signals. For the frequency band used in seismic exploration, petroleum engineering, and local security applications, such discrete nonstationary sources generating coherent signals are a primary cause of interfering noise generally called *clutter* in sonar and radar systems.

Seismic arrays for global monitoring are traditionally clustered sensors deployed at spacings that enable the analysis of the received signals as a wavefield (Ammon *et al.*, 2021). Arrays having apertures of several kilometers to ~25 km for regional monitoring have been integrated into the global seismic monitoring infrastructure over the last ~50 years. Local area monitoring applies these concepts for industrial and security applications for areas ranging from 10s of meters to 10s of kilometers using local passive seismic arrays with element spacings on the order of meters and apertures on the order of 10 meters or smaller (*e.g.*, Tinker *et al.*, 2021).

Using analog receiver groups for exploration seismology predates WW2. Some early papers on the development and use of these analog arrays in active seismic surveys include Rieber (1936), Klipsch (1936), and Johnson (1939). At this early stage in the development of seismic exploration techniques it was recognized that geometric arrangements of sensors offered a way of reducing

the coherent noise originating at shot points. Both the advantages, the problems, and the physical and mathematical description of using receiver groups of a fixed design have been explored in the nearly 100 years since (e.g., Smith 1956; Denham 1963; Newman and Mahoney, 1973; Cordsen *et al.*, (2000), Baeten *et al.*, (2001), Cortes *et al.* (2015), Dean *et al.*, 2015).

The fixed-design linear analog arrays employed for receiver groups in active surveys provide a single response pattern for emphasizing plane waves reflected from a deep layer such that the angle of incidence on the horizontal array is more vertical. The apparent wavenumber of narrow angle reflections will be low, compared to surface waves propagating from the shot point, so the receiver group functions as an analog low pass wavenumber filter (e.g., Newman and Mahoney, 1973). However, the array response is three dimensional and symmetric about the receiver group axis; any other noise energy arriving at a roughly broadside orientation to the array will also have a low apparent wavenumber and not be filtered. Therefore, to have a more general spatial filtering application, the analog array must be designed to take into account coherent noise arriving from multiple directions.

The move to single-sensor digital sensor data acquisition has influenced survey designs to enable more flexible processing post acquisition including true digital phased array processing (e.g., Roux *et al.*, (2014)). Nevertheless, it is important to understand that both the global monitoring mission and the exploration applications primarily have used two dimensional arrays in linear or planar geometries, with responses best described as a function of apparent velocity, apparent slowness, or apparent wavenumber.

Array Requirements and Array Design Considerations

The beamforming operation in phased array processing shifts the relative phases of the acquired data such that signals recorded by each sensor can be aligned (via time delay/advance) and summed to maximize the power of the received signal propagating across the array in a specific direction and with a specific speed compared to the incoherent noise and coherent signals arriving from other directions and/or at other speeds. This beamforming operation decomposes the wavefield into directional components oriented along the defined beam main response axes (MRAs) such that signals originating from sources that are spatially apart can themselves be separated. Array SNR gain depends on the pairwise cross-correlation coefficients between the elements of the array; arrays of identical designs in differing noise fields will have different array gain (Urlick, 1983). Obviously then the gain of the array degrades as the signal coherence decreases or as noise coherence increases.

For the elements to be processed cooperatively as a phased array, the measured wavefield must be coherent across the array, and it must be equally measured across the array, implying that each element must be coherent in time, frequency and phase, and space with respect to the other elements in the array. Coherence in time dictates that all data acquisition components must be on the same clock or that differences between the clocks be much smaller than the final sample rate, and that no differential time delays are added to the measurements output by the sensors across the array. Coherence in time also requires then that there is little differential wavefield time distortion as the energy propagates from the source to the array; the temporal coherence factor in sonar and radar systems is an important consideration for dynamic media (e.g., Yang, 2006) but not a general concern for seismic applications.

Coherence in frequency and phase requires that the sensors have identical frequency and phase responses over the band of interest such that the sensor does not add any phase factors, shifts, or distortions to the received signal differing from that of any other array element. Likewise for sensors with a directional response, that the sensitivity patterns are identical from sensor to sensor and are aligned when emplaced. This also requires identical processing of the channels such that operations like channel equalization do not produce differential phase shifts.

Coherence in space dictates that the elements must be located with a precision much greater than a fraction of the shortest wavelength of interest, and that the array aperture be within a “coherence length” of the shortest wavelength of interest to not detrimentally affect gain. A *wavelength-normalized coherence length* is defined as the distance at which the pairwise coherence falls below $1/e$ and is estimated using the narrow-band coherence function, broadband correlation function, or coherent SNR gain from either pairwise direct measurements obtained from either a filled aperture or the steered beam response from a sparsely filled aperture (Cary, 1998). Factors affecting the coherence length also effect the beam width and array gain, and include multipath interference, and refractive and scattering effects attributed to inhomogeneities, interfaces, and roughness at interfaces (Cary, 1998). Scattering by inhomogeneities generate travel time fluctuations when considering wavefield arrivals at equidistant point sensors (Shapiro and Schwarz 1995; Shapiro and Schwarz 1996). The overall effect is that array coherence lengths are dependent on the signal propagation distance as well as wavelength.

The overall geometry and inter-element spacing d of the array elements (also known as stations in global seismology) are determined depending upon design frequencies f_d , media velocities c_p and c_s , coherence lengths, and the understanding of the noise field. Equally important considerations include the desired beam width, the directivity index or array gain, and response pattern variability with beam MRA orientation. The design wavelength is then $\lambda_d = c/f_d$ and the ideal element spacings d are derived from the design wavelength as $d = \lambda_d/2$. Because seismic propagation involves multiple types of waves traveling at different phase velocities, an array with a single element spacing d will correspond to more than one design wavelength.

For passive monitoring, a large array aperture is desired to provide a narrow beamwidth and a more precise estimation of the direction of arrival of the signal-of-interest (SOI) with a geometry largely designed to spatially sample the wavefield. However, arrays with aperture larger than the coherence length will not generate a greater gain since adding elements and increasing the aperture adds only noise to the resulting beam (Urlick, 1983). Therefore, the coherence length of the signal of interest is a fundamental limit to spatial coherent signal processing (Cary 1998). For a particular aperture, increasing the number of sensors and reducing sensor spacing with an accompanying increase in the design frequency will increase the gain so long as the noise remains uncorrelated between sensors. Likewise, then, the correlation distance, defined as the separation distance at which the pairwise coherence in the noise drops below a threshold usually set at ~ 0.5 and taken as the minimum spacing needed for a statistical independence of noise in the data, also needs to be considered as a fundamental limit (see for example, summary in Dean *et al.*, 2015). This correlation distance reflects the point at which increasing the number of sensors with a decreasing spacing has a diminishing return on the array gain due to the correlation of the noise.

The phased array design must also take into account the expected coherent clutter signals propagating throughout the monitored volume. As discussed in Strobba *et al.* (2022) and Krohn *et al.* (2008), including sources of coherent noise in survey planning is being more commonly considered. It may be impossible to come to a complete count and review of the publications in the last 50 years focusing on the many aspects of seismic noise and the ensuing discussions covering both monitoring and exploration applications. Nevertheless, a simple, common observation is that in many geologic carbon storage monitoring sites, the coherent noise will be huge and have no stationary spatial preference. To summarize then, a primary design goal for a phased array is to create the largest aperture warranted under the coherence length, using the array element separation that is warranted under the correlation distance, for suppressing the noise wavefield and separate clutter signals, given the required design frequency and bandwidth.

SADAR Array Design

The SADAR arrays are referred to as “compact volumetric phased arrays” to distinguish the designs from extended linear or planar sensor deployments, or combinations thereof. The arrays are compact both when compared to surface deployment areal coverages and mathematically; the set of array elements at the greatest distances from the array centroid form the vertices of a convex polytope.

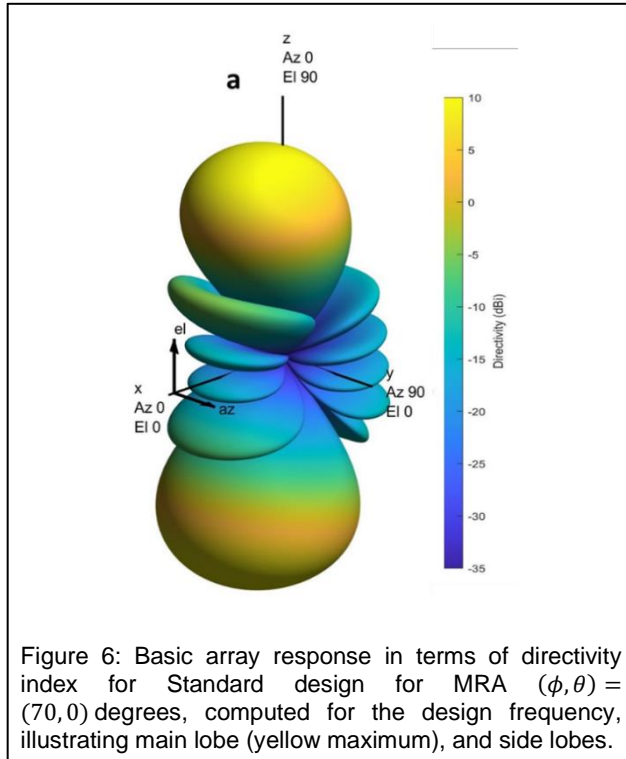
The geometry of a basic compact volumetric phased array is shown in Figure 4 as a uniform cylindrical array with a center column. The total aperture of the array is set within an expected coherence length for the design frequency and the medium wherein the array is emplaced, and the expected geometry of the wavefronts associated with the signal of interest. The UCA of Figure 4 takes advantage of two primary design frequencies, yielding two fundamental element spacings based on the radius and spacing between levels for P waves (in this example). Nevertheless, the diversity in pairwise element spacing across all 54 elements provides an overall broader band array response pattern.

In phased array design, array response patterns are typically computed in terms of directivity index as a function of azimuth and depression (i.e. dip) angles for understanding the beam width and side lobe response. Array response patterns are commonly shown in two dimensional plots resembling typical antenna patterns, as a function of frequency, wavelength, or wavenumber, or their apparent counterparts, and horizontal and vertical angle of arrival of the signal (e.g., Newman and Mahoney, 1973; Havskov and Alguacil, 2006; Schweitzer *et al.*, 2012; Douglas, 2013). Nevertheless, the array response is three dimensional even for two dimensional arrays.

The basic array response pattern shown in Figure 6 in terms of directivity index for the array of Figure 4 appears as a complex solid. The pattern is given for a single frequency, close to the design frequency. The response pattern illustrates that using the SADAR arrays enables mitigation (i.e. rejection) of coherent signals arriving from arbitrary directions and separation of unrelated simultaneously-arriving-signals that cover the same frequency spectrum but that originate with sources at different locations using beams with different MRAs, none of which is possible with small aperture or small element count arrays (e.g., Swanson and Culver, 2017).

However, the spatial filter provided by phased array processing is never perfect as the side lobes in Figure 4 demonstrate. Main lobe – side lobe relative height and nodal response placement may be modified using a variety of approaches. Nevertheless, the derived beam having MRA aligned with the angle of arrival of the signal provides the optimal SNR for estimating the received signal.

Furthermore, sampling the incident wavefield in all three dimensions allows the direct measurement of the arriving signal phase velocity. Linear arrays produce a directional ambiguity in azimuth and depression angle (dip) about the array axis, as well as limiting velocity resolution to “apparent velocity.” Circular and patch arrays deployed along the surface remove the azimuthal ambiguity but not the ambiguity in depression angle because of reliance on apparent velocity. Furthermore, for any planar array deployed along the surface, as the incident wavefield approaches vertical, any phase velocity resolution is lost.



For SADAR arrays, the number of elements and spacing of boreholes is set to provide a uniform azimuthal response pattern and a desired gain, depending on the estimated statistical independence of the noise in the channel down to $\frac{1}{4}$ of the design wavelength, as well as considerations on the economics of permanent installation in multiple but relatively shallow boreholes. The depth of the top-most sensors is set considering the near-surface noise, near-surface geology, and stratigraphic layering over the vertical aperture of the array. The network of arrays is designed based on the estimated performance of the individual arrays, discussed below.

System Analysis

This description of the received signal is presented from the perspective of the sensor (or receiver) located at a fixed point (x, y, z) and receiving a field of energies containing a mixture of the signal of interest and competing clutter signals as well as a variety of environmental noise processes. The response of the individual sensors to the total wavefield is the measurement of the received signal, modeled using the standard approach as a linear function of present and past values and independent noise processes but in consideration of the cluttered operating environment:

$$y(t, f) = \sum_k [s_k(x, t, f)] + n_a(\dots) \quad (1)$$

where $s_k(x, t, f)$ is the received coherent signal from any number k of discrete SOI or clutter sources, and $n_a(\dots)$ is the additive noise encompassing all noise processes in the environment (where \dots represents combinations of the time, frequency, and/or spatial domain). Depending upon wavelength, $n_a(\dots)$ may be correlated between elements and may not be azimuthally isotropic or random in phase. In general, $n_a(\dots)$ is not diffuse (e.g., Mulargia, 2012).

An expansion of the model is convenient for categorizing the types of noise and signals:

$$y(t, f) = S(x, t, f) + \sum_k [s_k(x, t, f)] + n_a(t, f) + n_a(f) \quad (2)$$

where $S(x, t, f)$ is one of the received SOIs in the defined analysis frame originating from a source of interest, $s_k(x, t, f)$ represents all the undesired k coherent clutter signals received simultaneously and from multiple directions, $n_a(t, f)$ is the non-stationary additive noise, and $n_s(f)$ is the stationary additive noise. For the purposes here, stationarity is considered up to order 2 over a time of several analysis frames such that a stable estimate of the probability distribution is possible (Priestley, 1981). *Non-stationary* then can be considered as an “instantaneous” measurement over a single analysis frame and does not have restrictions on its distribution function. If k is a small number and clutter sources are widely spatially separated, it may be possible to reduce the coherent clutter signal term to a simple quantifiable term $n_{ac}(x, t, f)$, but that is not the general case without quantifying these components, and usually will be changing even over the course of a few hours.

Given $y_i(t, f)$ the suite of received signals from the individual array elements i with locations (x, y, z) as illustrated in Figures 4 and 5, let $\Psi()$ represent processing operations acting across all $y_i(t, f)$ for an analysis frame such that a processed continuous series $\alpha(t, f) = \Psi(y_i(t, f))$ may be derived. For example, $\alpha(t, f, \phi, \theta)$ may represent the series from a beam processed to emphasize a MRA along the vector (ϕ, θ) from the array centroid aligned with the direction of arrival of our particular $S(x, t, f)$. The noise in $\alpha(t, f)$ and the coherent clutter signals $s_k(x, t, f)$ not aligned along the beam MRA are suppressed by whatever series of operations comprise $\Psi()$, but the coherent signal $S(x, t, f)$ is largely unmodified.

The primary problem becomes identifying $S(x, t, f)$ and extracting or deriving characteristics and information pertinent to $S(x, t, f)$ from $\alpha(t, f)$ in the presence of competing and interfering unknown signals originating from sources that are not of interest, all embedded within a variety of unknown noise. To parameterize this problem, we follow sonar system analysis as given in Urick (1983), Burdic (1991), Ainslie (2010), and Abraham (2019) among others. The sonar description development is easily recognized as sharing commonality with Boatwright and Choy (1986), Choy *et al.*, (2001), and Boatwright *et al.*, (2002). Following a signal detection paradigm, some measure of the presence of the signal derived from $\alpha(t, f)$ is required to detect the presence of the SOI, and then that measure must surpass a minimum threshold to achieve a required probability-of-detection. For example, a common approach includes the short-term average power written $|\alpha(t, f)|$. Casting a metric in terms of SNR power \mathbb{S} (as a function of frequency),

$$E[\mathbb{S}] = \frac{|\alpha(t, f)|}{E[\text{noise}(\alpha(t, f))]} \geq \text{threshold} \quad (3)$$

where $E[\cdot]$ is the expectation operator, it is obvious that the noise power component of the denominator representing the estimate of the ambient noise present in the derived series $\alpha(t, f)$ must be statistically estimated over several analysis frames, and the signal component in the numerator is contaminated by the instantaneous noise of the current analysis frame. It is common practice to cast the detection equation expression into decibels yielding:

$$10 \log_{10}[E(\mathbb{S})] \geq 10 \log_{10}(\text{threshold}) \text{ dB re: power} \quad (4)$$

or using the common symbol "DT" for the detection threshold in decibels

$$10 \log_{10}[E(\mathbb{S})] \geq \text{DT dB re: power} \quad (5)$$

The signal excess SE can then be defined as the portion of the SNR power that is greater than the detection threshold as a general measurement of the amount of signal we have to work with.

$$SE = 10 \log_{10}[E(S)] - DT \quad (6)$$

Rewriting the detection equation (5) and breaking the SNR power into individual factors yields:

$$DT \leq (SL - RP) - PL - (NL_f - AG - SP) + PG \quad (7)$$

where SL is the source level; RP is the radiation pattern of the source; PL is the propagation loss, a compound term; NL_f is the noise spectrum level, a compound term; AG is the array gain, SP is the sensitivity pattern of the sensor element itself; and PG is gain due to signal processing after the initial beamforming stage but still considered part of $\Psi()$. The radiation pattern factor RP acts as a modifier to the source level SL and is 0 dB for isotropic source; herein we will consider RP as lumped together with SL . The sensitivity pattern factor SP is equal to 0 dB for an omni-directional receiver but needs to be computed for dipole receivers; for our purposes here, we will neglect SP . In these types of gross parameterizations, frequency dependence is implicitly considered in each term, and a specified frequency band accompanies whatever numbers are reported.

Building from equations (6) and (7), the expression for signal excess becomes:

$$SE = [(SL - RP) - PL - (NL_f - (AG + SP)) + PG] - DT \quad (8)$$

Equation (8) directly defines the trade-off space of the independent factors for determining the ability of the system to detect $S(x, t, f)$. Signal excess "SE" is directly proportional to the performance of the system; as signal excess drops below 0 dB, the ability of a system to detect and locate a source will also vanish. In other words, equation (8) is a primary model of the system performance (system performance equation).

The noise level factor can be further parameterized as discussed regarding equation (2)

$$NL_f = 10 \log[n_a(f) + n_a(t, f) + n_{ac}(x, t, f)] \quad (9)$$

where $n_{ac}(x, t, f)$ represents the components of the coherent clutter signals $s_k(x, t, f)$ that the signal processing operations $\Psi()$ were unable to mitigate. It may or may not be possible to estimate the individual components of NL_f prior to performing in situ measurements, but it is always possible to measure NL_f and come up with a statistical estimate of the combined noise. The importance of the noise terms should not be underestimated because the detection of a SOI will be noise limited. In most cases, and especially for surface sensors, the noise will be dominated by the ambient seismic background with power that falls off as $1/f$. However, at high frequencies the noise limitation may be imposed by the self-noise of the sensor and instrumentation, addressed in following sections.

The propagation loss term, written as a factor in the denominator of the SNR, can also be separated into physical mechanisms contributing to signal power loss. The purpose here is not to correct a measurement or a waveform for loss, but to account for loss to better model the performance of the acquisition and processing pipeline system. Propagation loss nominally is defined as the ratio of $I(r)$, the intensity of the wavefield at an arbitrary point, to I_0 , the intensity of the wavefield at a reference distance, written as $loss = I(r)/I_0$ such that taking the propagation loss into decibels yields:

$$PL = 10 \log\left(\frac{I_0}{I(r)}\right) \text{ dB} \quad (10)$$

Given spherical spreading, the intensity at some arbitrary point is then:

$$I(r) = \{I_0 r^{-2} \exp(-2\pi r f / (Q_m c_m))\} * \prod_{k=1}^N (T_k)_m \quad (11)$$

where r is the range, c_m is the material velocities for propagation mode m , Q_m is the frequency independent factor for the energy dissipation properties of the media for propagation mode m , and T_k is the transmission coefficient for the wave at interface k between layers i and j for N discrete geologic boundaries between the source and receiver. For the cases discussed here, the propagation mode will be either P or S and we will not treat converted modes. The expression inside the curly braces is similar to the expression used in passive sonar, but the factor T_k representing transmission across boundaries is specific to solid earth problems. Similar elements in this expression can be found in Ammon *et al.* (2021) and Boatwright *et al.* (2002).

The propagation loss PL for spherical geometric spreading becomes:

$$PL = 20 \log r + 10 \log[\exp(2\pi r f / (Q_m c_m))] - 10 \log \left[\prod_{k=1}^N (T_k)_m \right] \quad (12)$$

The last term we label as *Transmission Factor TF* and is intended to capture simple scattering losses at interfaces. In these cases, the goal is a general estimate of the losses at discrete boundaries using geometrical ray theory transmission coefficients rather than precise corrections for estimating source energy. Transmission factor then is more appropriately parameterized as:

$$TF = 10 \log \left[\prod_{k=1}^N T_{k(i,j)}(p, c_{i,j}, \rho_{i,j}) \right] \quad (13)$$

explained as the product of N transmission coefficients $T_{k(i,j)}$, where $T_{k(i,j)}$ is defined for the k^{th} discrete boundary between geologic layers i and j for N geologic boundaries lying between the source and receiver as a function of ray parameter p , and the appropriate mode velocities c and material densities ρ for layers i and j .

Written in compact form, propagation loss is then:

$$PL = GS + AN + TF \quad (14)$$

for geometric spreading GS , attenuation AN , and transmission factor TF losses.

Observations and Analysis

Taking Equation (8) as the model for system performance, considering RP lumped together with SL , and neglecting sensor sensitivity pattern SP , six main degrees of freedom are identified. The source level SL , propagation loss PL , and noise level NL_f are the three main uncontrolled factors all depending on the physical system prior to data acquisition. The propagation loss PL , and noise level NL_f act directly to reduce and obscure the SOI. The factors of array gain AG , other processing gain PG , and the detection threshold DT represent the system components up to and including signal detection that can be controlled to affect the signal excess SE and register a detected signal.

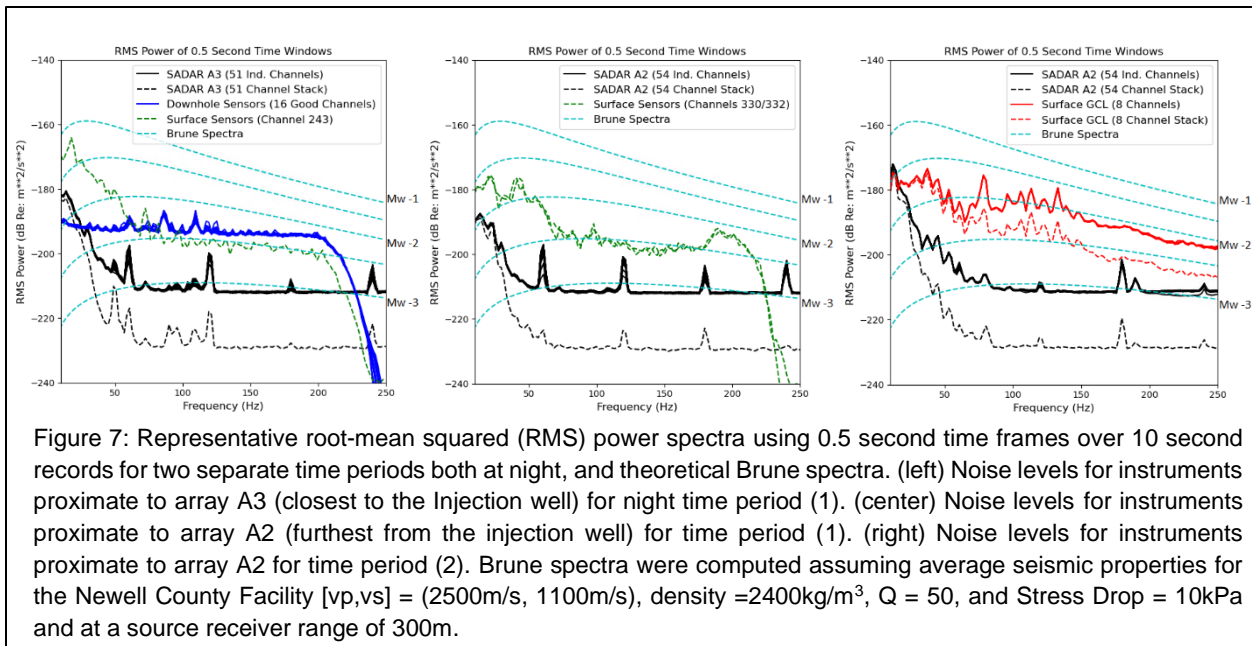
Examining the noise level NL_f , there are limited methods available for mitigating the combined noise. For sparse, single sensors in passive monitoring configurations, the most effective way to minimize recorded noise levels is to place sensors at depth to reduce the influence of surface

related noise. Although frequency band filters are always an option, there is no option for filtering based on wavenumber using single sensor emplacements. However, a phased array designed for a specific range of seismic wave frequencies and propagation speeds enables arbitrary directional beamforming, allowing the level of noise components that have uncorrelated frequency-phase-time relationships and randomized wavenumber attributes to be reduced via averaging across the array channels.

Figure 7 summarizes results comparing the noise levels of SADAR arrays against the other seismic instruments located at the NCF and shown in Figures 3 and 4. For our purposes here the individual noise terms in equation 9 are lumped into the noise level NL_f . The temporary surface GCL-3C geophone cluster (in red, Figure 7 right graph) and the permanent 3C geophones closest to the SADAR arrays (in green, Figure 7 left and center graph) record elevated noise spectral levels compared to single channels of the A3 and A2 SADAR arrays (Figure 7 in black). Our experience at the NCF indicates this difference is typical for the variety of noise conditions at the site. The spectra for the downhole array shown in blue in Figure 7 (left graph) appears to have an elevated noise floor compared to the other systems. We expect that this is the result of non-optimal acquisition settings that have pushed the noise floor above the ambient noise levels in the borehole and as such we perform no further analysis on the downhole array for this work.

Neglecting the downhole array, all spectra indicate a region of ambient seismic noise between 0Hz and at least 70Hz where the levels fall off with frequency, transitioning to an approximate steady-state noise floor above 100Hz for the SADAR arrays and permanent phones (left and center graphs, Figure 7). The spectra for the surface-emplaced GCL cluster eventually transitions to approximate steady-state noise levels above ~400Hz (not shown). We expect that the approximate steady-state noise levels reflect the combination of sensor and acquisition system self-noise processes, which should have basically gaussian distributions.

The difference in noise levels for the single channel surface and near-surface sensors compared to the single channels of the SADAR arrays for the band 30Hz-100Hz is between ~15dB-25dB for the GCL sensors and A2 and averages ~19dB for the geophones at 1m depth. For frequencies greater than 100Hz the difference in the noise levels on the GCL cluster single channels and the A2 single channels ranges between ~8dB-16dB, and for the geophones at 1m depth the average is ~13dB. This reduction in NL_f between the single geophones and the individual sensors for the SADAR arrays is provided by increasing emplacement depth alone.



The channels in the SADAR arrays and the GCL cluster were then stacked to form the incoherent trace, and the spectra were determined as shown in Figure 7. The result of the incoherent summation for the SADAR arrays is an indication of array gain but does not include the gain due to the directional wavenumber filter that beamforming provides. The resulting spectra for the SADAR arrays, shown as the black dotted line in Figure 7 graphs, indicate that steady state noise level above 100 Hz is suppressed by ~ 17 dB compared to the SADAR array single channels, which agrees with the theoretical $10 \cdot \log(N)$ figure (Urlick, 1983). The spectra of the incoherent summation for the GCL cluster, shown as and the red dotted line in Figure 7 right graph, indicates that, although the sensors were located within a distance that should preclude noise independence, at frequencies greater than $\sim 90\text{Hz}$ there are some random components of the noise that are suppressed by ~ 6 dB; less than what would be expected for uncorrelated noise.

Looking in the band 40Hz-100Hz, which is the main band for detecting microseismic events at the NCF, and comparing the gain against noise for the SADAR arrays using the incoherent sum vs. single channel measurement, for A2 the gain against the noise is 8-17dB and for A3 gain averages $\sim 16\text{dB}$. In this same band, Figure 7 (left and center) shows the difference in the noise spectra from the incoherent sum for the SADAR arrays compared to the near-surface geophones averages $\sim 36\text{dB}$ for A2 and $\sim 34\text{dB}$ for A3. The conclusion follows that these gain estimates over the single channel surface emplacements are due to the combination of deploying the arrays at depth and the coherent processing array gain.

The NL_f spectral level in the frequencies below 30Hz is dominated by more coherent ambient seismic noise and clutter signals. This band is at least a factor of 3 below the lowest array design frequency so we would not expect any significant noise suppression from an incoherent sum because at corresponding wavelengths the noise on the separate channels should not be independent. We infer that the gain over the single channel emplacements in this band is due to emplacement depth alone.

The incoherent sum for the SADAR arrays plotted as the dotted black line in Figure 7 represents the summed effect of the noise level NL_f from all contributions and the array gain AG . As stated in Equation (8) for mathematical performance, the ambient and clutter noise factors limit ability of a passive seismic monitoring system to detect, locate, and measure microseismic events. Spectra for microseismic events (Brune, 1970, 1971) as shown in Figure 7 were computed assuming average seismic properties for the Newell County Facility $[v_p, v_s] = (2500\text{m/s}, 1100\text{m/s})$, density $=2400\text{kg/m}^3$, $Q = 50$, and Stress Drop = 10kPa and at a source receiver range of 300m. These modeled spectra illustrate that even under ideal background noise levels the surface sensors would struggle to detect events smaller than $M_w -2$. However, Figure 7 illustrates that the network of SADAR arrays are able to acquire signals that, when processed to generate the optimal beamformed trace, have sufficient signal excess SE to automatically detect the event, identify phase arrival times, and perform a location, for $M_w -2.5$ events occurring throughout the monitored volume.

Equation (8) also illustrates that the propagation loss PL factor acts against the source level SL . The terms that contribute to the propagation loss are functions of range as shown in Equation (12). Detection performance versus range therefore includes PL and can be estimated from the bulletin of located events (Zhang *et al.*, 2022; Zhang *et al.*, 2023) in light of event size and the measured peak received signal values measured from the optimal beam. The goal is to examine the received signal power at each array measured from the optimal beam as a function of the event source level (i.e. magnitude) versus event-to-array range for events with low location uncertainty, as shown in Figure 8. Using 50 located high-confidence events with good SNR having maximum ~ 20 m semi-major axis uncertainty and maximum ~ 30 meters uncertainty in depth, yields one measurement per array for a total of 200 measurements, but they cannot be considered as completely independent.

For purposes of showing magnitude-range detection characteristics, example curves of theoretical signal power versus range are plotted as dashed black lines overlaying the Figure 8 scatter plot assuming geometrical spreading is the only source of propagation loss. Also plotted are the measured average individual channel noise power levels for all SADAR arrays (red dashed line) and then the approximate values for noise levels taking into account the gain measured in the optimal beam for ~ 10 dB minimum gain to ~ 18 dB maximum expected gain over the single channels (green dashed line and dot-dash line respectively).

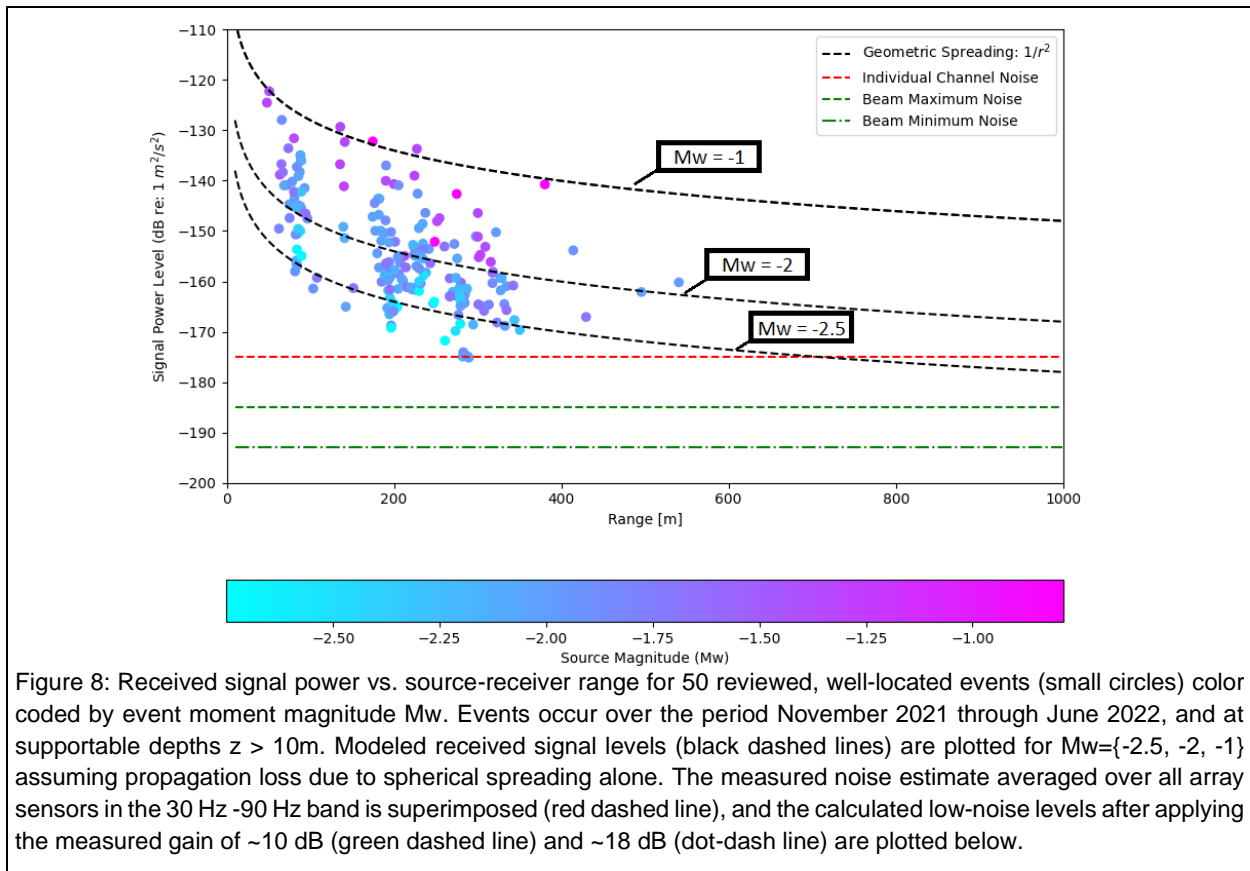


Figure 8: Received signal power vs. source-receiver range for 50 reviewed, well-located events (small circles) color coded by event moment magnitude M_w . Events occur over the period November 2021 through June 2022, and at supportable depths $z > 10\text{m}$. Modeled received signal levels (black dashed lines) are plotted for $M_w = \{-2.5, -2, -1\}$ assuming propagation loss due to spherical spreading alone. The measured noise estimate averaged over all array sensors in the 30 Hz -90 Hz band is superimposed (red dashed line), and the calculated low-noise levels after applying the measured gain of $\sim 10\text{ dB}$ (green dashed line) and $\sim 18\text{ dB}$ (dot-dash line) are plotted below.

The fused information shown in Figure 8 suggests that for events with $M_w \leq -2.5$, reliable detection requiring a signal excess peak signal power of $SE \geq \sim 10\text{ dB}$ and a high confidence location of maximum $\sim 20\text{ m}$ semi-major axis uncertainty and maximum of $\sim 30\text{ meters}$ uncertainty in depth, is limited to a maximum range between 600 and 800 meters. This in turn suggests that the M_w magnitude of completeness for the SADAR system bulletin of locatable microseismic events limited to the volume covered by the SADAR network should not be greater than about $M_w = -2.5$. Moreover, the upper dashed green line in Figure 8 also suggests that the threshold for event detection at any individual SADAR array at source-receiver ranges out to 800m is substantially lower than $M_w = -2.5$, which roughly agrees with the estimates of event detectability for the Brune models plotted in Figure 7.

Conclusions and Outlook

A sparse network of four permanent SADAR compact volumetric phased arrays that Quantum Technology Sciences installed at the CaMI Newell County Facility has demonstrated a robust capability for continuous passive monitoring of microseismic events over the past year. The general approach for using sparse networks of SADAR arrays as a critical yet relatively inexpensive MMV technique for GCS is now proven, and quantifying the performance of the hardware and software systems for continuous MMV is now one of the priority tasks. The year-long continuous seismic signal collection allows assessment of several of the factors impacting

phased array and network performance for microseismic event detection and location. A mathematical performance model based on the sonar equation framework aids in understanding the factors contributing to the signal-to-noise ratio that limit detection, and consequently the ability of any system to locate and characterize microseismic events.

The four SADAR arrays comprise a total of 231 channels yet occupy only ~150 m² total on the surface. In terms of noise suppression and SNR improvement metrics, the observed performance heavily favors coherently processed SADAR arrays. Measurements indicate that coherent processing of the data acquired using SADAR phased arrays provide noise level suppression from 10dB to ~18dB over individual array channels. The total measured noise suppression of beamformed SADAR arrays over the closest surface stations is at least ~30dB, reflecting the combined effects of moderate emplacement depths and coherent processing.

In terms of continuous microseismicity monitoring, the SADAR network and processing system reliably locates microseismicity at least down to $M_w \approx -2.5$ at source-receiver ranges that extend 600m-800m. Signal levels versus range comparisons with noise levels suggest that $M_w = -2.5$ is the lowest magnitude of completeness for locatable events. However, both the measured received signal versus range and the estimates of expected signal spectra using the Brune (1970, 1971) model suggest that the limiting threshold for event detection is substantially below that magnitude.

These measured performance examples combine factors from the performance model. Noise level NL_f and array gain AG are lumped together to produce the noise estimates shown in Figure 7; source level SL and propagation loss PL are lumped to produce the received signal power estimates of Figure 8. The continuation of this work is then to complete the analysis and produce estimates of the individual performance equation factors as well as breaking out components of the noise level and propagation loss as represented in Equation (9) through Equation (14). The next goal using this model framework is estimating the source level detection and location thresholds as a function of depth throughout the monitored volume to arrive at a complete performance assessment.

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